Machine Learning and the Digital Era from a Process Systems Engineering Perspective

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SNE 32(1), 2022, 29-36, DOI: 10.11128/sne.32.tn.10595
Received: 2020-11-10 (Selected EUROSIM 2019 Postconference Publication); Revised: 2021-09-14; Accepted: 2021-10-05
SNE - Simulation Notes Europe, ARGESIM Publisher Vienna
ISSN Print 2305-9974, Online 2306-0271, www.sne-journal.org

Abstract. Modern sensorization, communication and computational technologies provide collecting and storing huge amounts of raw data from large cyber-physical systems. These data should serve as the basis to take better decisions at all levels (from the design to operation and management). Nevertheless, raw data need to be transformed in useful information, usually in the form of prediction models. Machine learning plays a key role in this task. Process industry is not alien to this digital transformation, although large processing plants present particularities that differentiate them from other systems. These differences, if neglected, can make machine learning for general purpose fail in extracting the right information from data, leading thus to unreliable process models. As such models are the basis on which the ideas towards the cognitive plant rely, this issue is of major importance for a successful full digitalization of the process industry. In this paper the authors discuss these aspects, as well as some suitable machine-learning approaches, through their experience gained from applying advanced engineering in an industrial case study.

Introduction

In the digital era, the impressing amount of data that can be stored, as well as the speed at which they can be stored, are expected to significantly impact the decision-making procedures at all levels of a factory: from the process design, through the operation and maintenance, to production scheduling and supply chain. Coordinating actions at all levels is the work towards reaching the full digitalized, cognitive and, ultimately, autonomous plant.

However, in the process industries (those that process bulk materials or resources to transform them into products), these expected advances will not come alone by just collecting huge amounts of data and presenting them in a nice view: data treatment and analytics is necessary to ensure the data quality. Moreover, models for reliable predictions need to be built upon such data, in order to be later used in advanced control, optimization and planning routines [1].

Once data quality is ensured, models are to be build, and the current trends from the big-data revolution seem to impose the wide set of machine-learning (ML) techniques in all sectors. However, as the authors will illustrate in this paper, the direct application of an ML approach to a modelling problem in the process industry needs to be evaluated carefully.

In this particular sector, production takes place in a set of complex (and expensive) process units, linking flows of materials and energy at large scale. Nonetheless, the process industry is not characterized by a scarce knowledge on the involved processes: researchers on Process Systems Engineering (PSE) [2] have been developing physical models (e.g., distillation columns) for design, simulation and decision-support solutions during several years. Although these models have limitations for use in real-time applications (computational complexity and/or fitness to actual plants), it is not sensible to throw out all this deep knowledge and replace it by deep learning machines [3]. Thus, one of the key challenges of ML to successfully penetrate in the process industry is developing methods and tools that are able to naturally embed the existing physical knowledge on the underlying processes.

Researchers in PSE have already taken some steps forward in this path:

a) developing hybrid or grey-box models (combination of first-principles laws and regression equations) which get a high matching level with the actual plant [4];
b) proposing methodologies for robust data analysis/ reconciliation [5]; and
c) presenting approaches/tools for data-driven modeling that are tailored to the features of the process industry [6], [7].

In the following sections, the authors discuss the above-mentioned issues with ML through an industrial case study that consists of building a prediction model for the fouling accumulation in the heat exchangers of a multiple effect evaporation plant. Some of the recently proposed methodologies and software are tested on this case study, trying to give the reader a clearer vision on the potential advantages as well as the existing limitations.

1 Description of the Case Study and Motivation

The case study is an evaporation plant in a cellulose fiber production factory, whose objective is to continuously remove certain amount of water from an acid liquid inlet (called *spinbath* hereinafter) that comes from spinning machines, the place where cellulose pulp is recovered into fibers of desired properties.

The plant layout, simplified in Figure 1, makes use of several heat exchangers in serial connection to heat the spinbath up to a temperature suitable to start the evaporation by pressure drop. This pressure drop is first created in the evaporation chambers by induced vacuum, and later by further condensation in an attached surface condenser, creating thus a multiple-effect evaporation. The efficiency of these type of plants (live-steam consumption per amount of evaporated water) is mainly determined by: 1) the performance of the cooling system and 2) the fouling state in the heat exchangers (due to deposition of organic residues present in the spinbath) [8]. Therefore, representative, but of limited complexity, models of these systems are needed to predict online the impact that the operation will have on the plant performance over time.

For such a task, a set of experiments were performed running the plant and the cooling system in different operating conditions (setting different values for the main control variables: spinbath flow, temperature set point, cooling water flow). Moreover, in order to get information on the fouling degradation in the exchangers over time, an extensive dataset corresponding to several months of operation (including stops for cleaning) has been also recovered from the collected plant historian.

In this way, the modeler may be tempted to directly try to find black-box models which relate the live-steam consumption with the input variables through raw measurements. This involves some risks and limitations, as we will see later on.

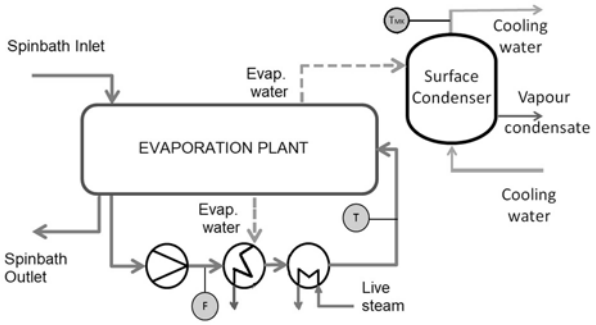


Figure 1: Schema of the evaporation plant with attached surface condenser as cooling system.

2 Data Conditioning and Variable Estimation

Everybody in the machine learning and data-analytics research community claims that ensuring the quality of data is essential to extract sensible information: process measurements need to be coherent and reliable. In industrial practice, however, it is not common to go beyond the standard filters to exclude faulty instrumentation (out of range sensors, communication loss, etc.) and to average data with the aim of mitigating the effect of noise to account for steady state in large-scale systems.

A systematic method to detect and assign the quality of process data can be proposed from the Spanish AENOR-UNE norm 500540 [9], used to analyze data in meteorological stations. This method is based on several progressive levels of tests where each datum is associated to the highest quality level being passed, see Figure 2. Note that the more restrictive tests (thus, the ones ensuring higher confidence data) are model based.

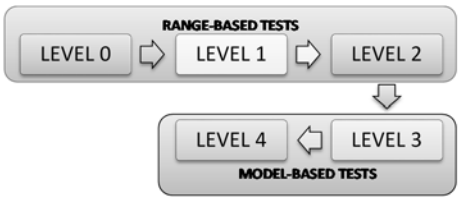


Figure 2: Data quality and validation levels.

Each level depicted in Figure 2 corresponds to the following quality tests:

- **Level 0: Communications.** Check whether the data are recorded or not at the expected sampling time (problems in the sensor or in communications).
- **Level 1: Limits.** Check that the datum is within instrument span and/or physical range. E.g., the maxi-

mum values expected of the flowmeters will be determined by a simple analysis of the flow capacity limit of the pipes.

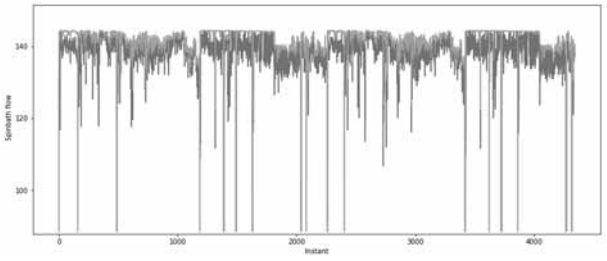
- **Level 2: Trends.** Consider the time changes of the data in consecutive sampling times. E.g., the level in a big tank cannot change faster than several centimetres by minute.
- **Level 3: Data reconciliation.** With a basic first-principle model of the plant, apply methods of (dynamic) data reconciliation (DR) and gross-error detection [5]. This provides a reliable set of measurements as well as estimations of unmeasured variables and parameters that are coherent with the process physics. E.g., mass balances need to be fulfilled in each time instant.
- **Level 4: Time series & correlations.** Consider the time series of the collected values for each variable [10]. E.g., a time-series model can be derived by analyzing the historical data of the flows in a pipe, relating them with valves, and the model output is later used to compare and validate newly recorded data.

Fuzzy logic and set theory can be used to develop filters for the three first levels, based on comparison rules which are able to remove inconsistent data [11]. Different strategies and rules can be used, such as range and speed of change of the measurements, etc. Nevertheless, what really makes the difference in the authors' opinion are the model-based tests, because they include process knowledge in the data processing. Of course, these involve higher engineering effort for implementation, as relatively complex models of the plant/process (either first principles or time series) need to be previously build.

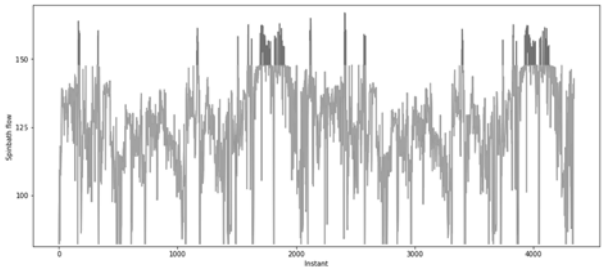
After these quality tests, resource and key efficiency indicators can be defined upon reliable sets of measurements to monitor the plant efficiency in real time [12].

2.1 Instrumentation Issues and DR in the Evaporation Plant

When retrieving sensor data from the historian, the first issues usually arise: many of the collected flow measurements were either "upper bounded" by the instrument range (span-related issue) or they were showing values higher than the actual flow, see Figure 3. In particular, this last problem was not caused by a biased instrument, but because of the improper location of the instrument itself: there was a bypass valve in the pipe after the flowmeter, so a (non-constant) undetermined part of the spinbath was sent to another equipment. Hence, the actual flow was usually lower.



a) Wrong measurement due to wrong sensor placement.



b) Actual values exceeding the instrument range.

Figure 3: Flow-measurement issues. Orange line: sensor values. Blue line: actual values.

Realizing of such wrong values and the explanation took the authors a significant amount of time and several failed modeling attempts. However, most of these data passed the tests of range-based filters. Here we highlight the importance of the model-based tests, because suitable DR of these wrong measurements with mass-balance equations plus the rest of plant measurements provided the corrected values depicted in blue in Figure 3.

Moreover, back to the end goal of predicting the fouling in the evaporation plant, we already encounter an additional issue: the long-term loss of efficiency, only reflected on a single output (the increase of live-steam consumption) is masked with the cooling system performance and the plant operation conditions (spinbath flow). Hence, the fouling effect is hardly identifiable by a direct ML approach with the available measurements.

To overcome this issue, we also recalled dynamic DR [5], including the energy balances in the plant model, to *estimate* the lumped heat-transfer coefficient $UA(t)$ in the exchangers over time [7]. ML techniques can be now applied to "discover" models upon these coherent estimations, also called *virtual measurements* in the soft-sensors related literature. Details provided in the next section.

3 Prediction Models and Constrained Regression

Once reliable values for all process variables (states x, outputs y and inputs u) are available, including coherent estimates of time-varying parameters and / or process un-

known inputs z, any ML approach (e.g., artificial neural networks [4], canonical partial least squares [13], support vector machines [14], etc.) can be, in principle, a good candidate to build plant surrogate models in the general form

$$y = f(\alpha; x, u, z), \alpha \in \mathbb{R}^n \text{ regression parameters,} \quad (1)$$

or submodels (equations being part of a larger model) relating some variables $z^* \in z$

$$z^* = g(\beta; x, u, z), \beta \in \mathbb{R}^m \text{ regression parameters,} \quad (2)$$

At this point, there is a fundamental question to discuss: Even having reliable datasets for regression, are "standard" ML approaches enough to guarantee black-box models whose response is coherent with the process physics? Thinking on it, the answer to that question is in general NO, and the reason is given next. If one outlooks the training methods used by common ML tools, you will find that most of them rely exclusively on data, and that the performance of the black-box model to train is basically defined by the fitness to such data (plus suitable regularization to avoid overfitting, of course). In this way, although the data are coherent with the process physics (passing the tests in Section 3) and the model achieves a perfect fit to such data, there is no guarantee that its response (even with regularized smooth models) takes values that do not violate basic physical principles at input values not contained in the training dataset. Indeed, a model can show good statistics (R2, RMSE, etc.) in validation datasets, but it may still "predict" negative flows out of the training region (extrapolation issues) or a non-monotonic response between consecutive inputs (interpolation issues).

As the end purpose of surrogate or grey-box models is to be used for decision support in (economic) control and optimization routines (hence, mainly for interpolation and extrapolation), the data-driven parts must be in accordance with the process physics [6], [15]. Therefore, some properties on the model response, such as bounds on the outputs and/or in their derivatives (monotony, curvature, convexity, etc.) would like to be ensured, not only over the regression data but in the entire expected region of operation. Therefore, ML in the PSE framework needs to be extended to include additional constraints on the model. Constraints which ideally need to be enforced on infinitely many points belonging to the (usually local) plant operating region. Here is where the concept of *constrained regression* plays a key role.

3.1 Constrained Regression

Assume that a dataset of N samples over time for some outputs y (or, equivalently, estimations of those z^* in (2)) and some inputs (x, u, z) is available. Then, a candidate model for regression $f(\cdot)$ is sought such that a p-measure of the error (e.g., L_1-regularized or least squares) w.r.t. the data is minimized over a set of constraints $c(\cdot)$:

$$\begin{aligned} &\min_{\alpha} \textstyle\sum_{t=1}^{N} \left\| y_{[t]} - f\left(\alpha; x_{[t]}, u_{[t]}, z_{[t]}\right) \right\|_p \\ &\text{s.t.}: c(\alpha; x, u, z) \leq 0 \; \forall \, x \in \mathcal{X}, u \in \mathcal{U}, z \in \mathcal{Z} \\ &\quad \alpha \in \mathcal{A} \end{aligned} \quad (3)$$

Note that the additional constraints $c(\cdot)$ specifying some desired features on the model response are *locally* enforced in a compact region $\Omega := \mathcal{X} \cup \mathcal{U} \cup \mathcal{Z}$ of the input space variables. These constraints may range from the simpler bounds on y ensuring, for instance, non-negativity, to the more complex bounds on the model derivatives (slope, curvature, convexity, etc.). Defined this way, (3) is a semi-infinite constrained nonlinear optimization problem, but it can be computationally tractable under some assumptions [16]. Next, the authors briefly present two approaches and software available to handle (3), jointly with a discussion on their advantages and limitations.

Symbolic regression. In this approach, the functional form of the candidate model is assumed to be unknown a priori. Instead, the algorithm seeks to construct it from a set of predefined basis functions $\mathcal{B}$, e.g. $\mathcal{B} := \left\{1, x, x^2, \frac{1}{x}, \log(x), e^{\tau x}\right\}$. Once this set is specified, the lowest complexity function $f(\cdot)$ that accurately fits the data is found from the selection of the more suitable basis in $\mathcal{B}$ via mixed-integer programming (MIP). The idea is to split the resolution of (3) in two stages: first, solving a data-driven constrained regression (i.e., $c(\cdot)$ is only checked on the points in the dataset) and, subsequently, testing the fulfillment of constraints $c(\cdot)$ by solving a maximum-violation problem with the model already fixed from stage 1. Hence, if a point on the input space is found to violate $c(\cdot)$ with the initially proposed model, such point is virtually added to the inputs dataset and the procedure repeats until no violation of the constraints is found in stage 2 [6].

If the *basis functions* are chosen such that they *are affine in decision variables*; note that this is a strong limitation for the selection of some nonlinear basis functions in practice, like $e^{\tau x}$ (its time constant τ needs to be fixed a priori, i.e., cannot be identified by the fitting algorithm); typically they are coefficients of a linear combination.

In this case, the problem to solve in stage 1 is computationally tractable (MIQP or MILP depending on the chosen norm for the regression error, i.e., $p = 1$ or $p = 2$). For example, for input variables x, problem (3) may become:

$$\begin{aligned}\min_{\alpha,\eta} \sum_{t=1}^{N} (y_{[t]} - (\alpha_0 + \alpha_1 x_{[t]} + \alpha_2 x_{[t]}^2 + \frac{\alpha_3}{x_{[t]}} + \\ \alpha_4 \log(x_{[t]}) + \alpha_5 e^{x_{[t]}}))^2 \\ \text{s.t.}: -\alpha_0 - \alpha_1 x_{[t]} - \alpha_2 x_{[t]}^2 - \frac{\alpha_3}{x_{[t]}} - \\ \alpha_4 \log(x_{[t]}) - \alpha_5 e^{x_{[t]}} \le 0 \;\; t = 1, \dots, N \\ \underline{\mathbf{a_i}} \eta_i \le \alpha_i \le \overline{\mathbf{a_i}} \eta_i \;\; i = 0, \dots, 5; \;\; \alpha_i \in \mathbb{R} \\ \eta_0 + \eta_1 + \eta_2 + \eta_3 + \eta_4 + \eta_5 \le T; \;\; \eta_i \in \{0,1\}\end{aligned} \tag{4}$$

In this way, the basis functions are active when the corresponding binary variable $\eta_i = 1$ and inactive otherwise. Model complexity is specified by a parameter T that is increased until a goodness-of-fit measure worsens. Afterwards, in step 2 an adaptive sampling methodology based on *derivative-free global optimization* techniques is used to identify points where the model is inaccurate and/or does not fulfill constraints - for the above case:

$$\begin{aligned}\max_{x} \;\; & \alpha_0 + \alpha_1 x + \alpha_2 x^2 + \frac{\alpha_3}{x} + \alpha_4 \log(x) + \alpha_5 e^x \\ \text{s.t.}: \;\; & x \in \mathcal{X}\end{aligned} \tag{5}$$

Note importantly that this problem is in general nonlinear and nonconvex.

This procedure is what the software ALAMO implements [18]. Although this approach involves iterations between MIP and NLP problems to global optimality (time consuming).

Sum-Of-Squares (SOS) regression. An alternative approach is casting problem (3) as a polynomial SOS optimization one [20] under mild assumptions. Of course, the main limitation of this approach is that the candidate models $f(\cdot)$ need to be polynomial in their arguments, i.e., the "potential set of basis functions" would be formed only by monomials in the input variables up to a predefined degree (the approach is recently extended in [19] to allow including some "smooth" non-polynomial basis via polytopic bounding). Nonetheless, paying this price worth it, because the resulting (single) optimization problem is *convex*, and the extra *constraints on the model* response and/or in its *derivatives are naturally enforced* (either globally, or locally in a region Ω defined by polynomial boundaries) with full guarantee of satisfaction, no matter how many samples are to be fitted, or which region was covered by the experiments. In this way, high-order polynomial regressors can be used with guarantees of well-behaved resulting function approximators, compared to most options in prior literature. For instance, a SOS version of the above (4)-(5) could be:

$$\begin{aligned}\min_{\alpha,\beta,\phi} \; & \textstyle\sum_{t=1}^{N} \phi_t \quad \text{s.t.}: \\ & \begin{bmatrix} \phi_t & \alpha_0 + \alpha_1 x_{[t]} + \alpha_2 x_{[t]}^2 + \alpha_3 x_{[t]}^3 + \alpha_4 x_{[t]}^4 \\ (*) & 1 \end{bmatrix} \succcurlyeq 0 \\ & t = 1, \dots, N; \phi_t \in \mathbb{R} \\ & \alpha_0 + \alpha_1 x + \alpha_2 x^2 + \alpha_3 x^3 + \alpha_4 x^4 \\ & \quad - s(\beta; x) \cdot (5^2 - x^2) \text{ is SOS } \forall\, x \in \mathbb{R} \\ & \underline{\mathbf{a_i}} \le \alpha_i \le \overline{\mathbf{a_i}} \;\; i = 0, \dots, 5; \;\; \alpha_i \in \mathbb{R} \\ & (\beta; x) \coloneqq \beta_0 + \beta_1 x + \beta_2 x^2, \beta_j \in \mathbb{R}, \text{is SOS } \forall\, x \in \mathbb{R}\end{aligned} \tag{6}$$

Here, well-known Schur complement and Positivstellensatz results (see [7] for details) have been used to cast the quadratic objective function (with extra decision variables ϕ) and the local enforcement of the constraint in a region $\Omega \coloneqq \{x: |x| \le 5\}$ (with extra decision variables β), respectively. Note that the highest degree of the polynomial SOS multipliers $s(\cdot)$ is chosen such that $\deg(s(\beta; x) \cdot (5^2 - x^2)) \ge d$, being d the degree of the candidate polynomial model to fit.

In this case, although no automatic selection of the suitable monomials among a potential set is done via MIP, note that standard regularization on the model coefficients α can be trivially included in the objective function, for instance with a metaparameter Γ that progressively weights the coefficients corresponding to high-degree monomials.

3.2 Application to the Case Study

Recall from Section 2 that the aim is to get data-driven prediction models of limited complexity for the cooling power and the fouling evolution in the plant.

Modeling the cooling power provided by the surface condensers. The actual cooling power can be computed from the data collected by the temperature sensors at the water inlet (T_{in}) and outlet (T_{out}) of the SC, and by the flowmeter measuring the volumetric water flow (F_{w}) send through the SC, as follows:

$$C_{\text{pow}} = \frac{4.18}{3600} F_{\text{w}} \cdot (T_{\text{out}} - T_{\text{in}}) \tag{7}$$

Thus, what is missing to fully predict the cooling power is a model that relates the outlet temperature T_{out} with the water flow F_{w} and the inlet temperature T_{in}.

To model that, a polynomial candidate function up to degree 3 in F_{w} was proposed to experimentally fit the recorded temperature difference $\Delta T \coloneqq T_{\text{out}} - T_{\text{in}}$ [21]:

$$\Delta T = \alpha_0 + \alpha_1 F_{\text{w}} + \alpha_2 F_{\text{w}}^2 + \alpha_3 F_{\text{w}}^3 \tag{8}$$

The fitting of (8) to the experimental data was done first by standard LS unconstrained regression, obtaining the resulting blue curves depicted in Figure 4. As it can be seen, when computing the cooling power with the obtained model, it shows a behaviour incoherent with the physics at high flows (region highlighted in the dashed box), i.e. the cooling power cannot decrease at higher flows. However, the model fitted the measured outlet temperature quite well (T_{in} was nearly constant during the experiments), with a monotonic response in fact, but this didn't avoid the wrong response in C_{pow}.

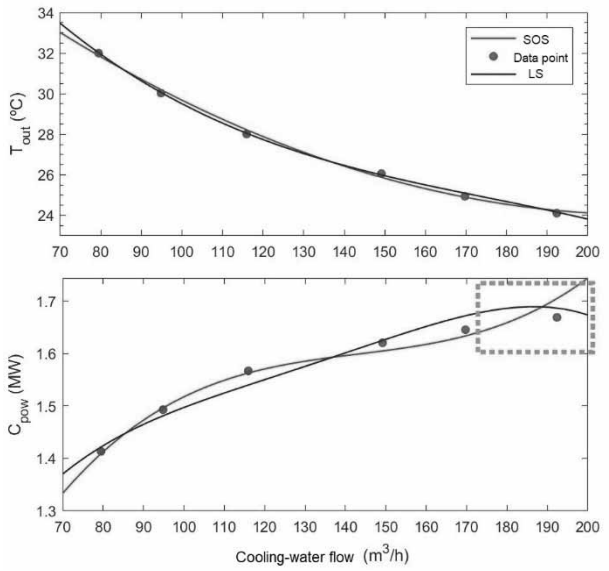


Figure 4: Fitting the cooling power developed by the SC at different water flows.

Then, SOS constrained regression was recalled in a second attempt, adding the constraint $\mathrm{d}C_{\text{pow}}/\mathrm{d}F_{\text{w}} > 0$ to enforce the known physical knowledge on the response. Note that derivatives of polynomials are also polynomials that can be directly checked for SOS. Now, the obtained model (red curves in Figure 4) behaves as expected, without showing any significant fitting degradation w.r.t the obtained by standard LS.

Modeling the heat transfer in exchangers. The goal here is to build up a model to predict both the influence of the spinbath flow F_{SB} and the operation time since last cleaning task t_{op} on the lumped heat-transfer coefficient UA (i.e. the fouling effect). Here the authors made use of the UA estimations provided by DR, already mentioned in Section 3 (omitted for brevity, see [7]).

The first issue arose when selecting sets for training and validation: although the recorded dataset looked huge (plant historian of 7-months length at 5-min. sampling time), the plant was usually running at high flows. Therefore, significant information of the convection and fouling behaviours at medium/low flows was missing.

In order to palliate this issue, a few experiments were executed on purpose when possible (normally it is not possible to "play" with an industrial plant in continuous production). Consequently, as often happens in the process industry, the authors thought that they will be facing "big-data stuff" in principle, but they ended up working with subsets of 22 samples for training plus 20 for validation, depicted in the figures below. This is nearly all the information available in the region of operation.

With this material, if no additional information about the process physics is included in the fitting problem, standard ML techniques fail in obtaining reliable black-box models in the regions where there is a lack of data to fit. See for instance problems of overfitting with standard LS in Fig. 5a, and problems of abrupt-falling responses (even going negative) where data is missing in Fig. 5b, despite using regularization techniques.

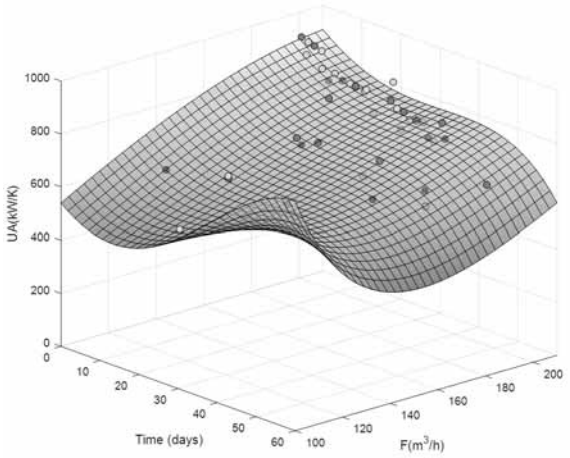
On the contrary, constrained regression in Section 4.1 fixed these modeling issues. We tested symbolic regression using the software ALAMO, with a large set of basis functions including monomials up to degree 4, rational powers, square roots, logarithms and exponentials. We also set up the additional constraint $f(\alpha; F_{\text{SB}}, t_{\text{op}}) > 200$ in the local-input region Ω. Thus, choosing the Akaike's criterion to avoid overfitting, we got the model (Fig. 6a):

$$UA = 2.27F_{\text{SB}} - 0.9095t_{\text{op}} + 84.978\log(F_{\text{SB}}) - 42.525\sqrt[3]{t_{\text{op}}} \tag{9}$$

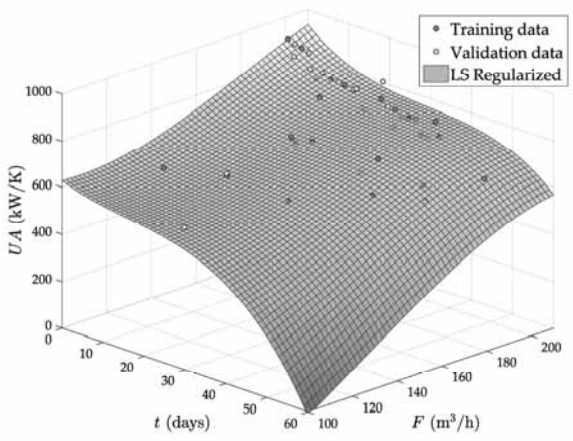
Going by the way of SOS constrained regression, proposing a candidate polynomial model of degree $d = 4$ and setting (local) bounds on its partial derivatives

$$0 < \frac{\mathrm{d}f(\alpha;F_{\text{SB}},t_{\text{op}})}{\mathrm{d}F_{\text{SB}}} < \lambda_{\text{F}}, \quad -\lambda_{\text{t}} < \frac{\mathrm{d}f(\alpha;F_{\text{SB}},t_{\text{op}})}{\mathrm{d}F_{\text{SB}}} < 0 \;\forall\, F_{\text{SB}}, t_{\text{op}} \in \Omega \tag{10}$$

to enforce a smooth and physically-coherent response, the model of Figure 6b is got [7].



a) Least-squares fitting



b) Least squares with regularization

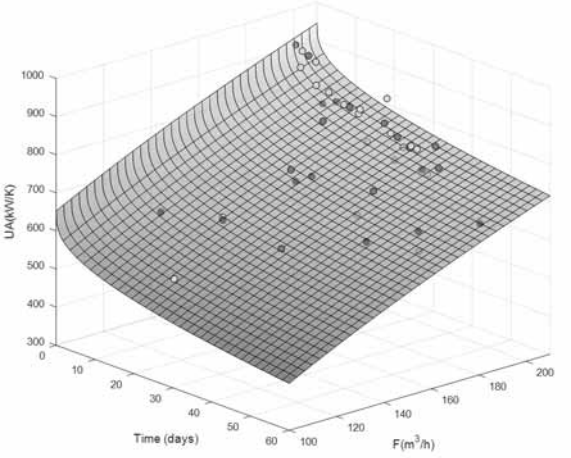
Figure 5: Fitting the heat-transmission coefficient by standard procedures.

Note that such model (11), got by SOS-constrained regression, keeps the desired physical features without incurring in significant fitness deterioration w.r.t. "the best" obtained by unconstrained LS regression with regularization, see the Table 1.

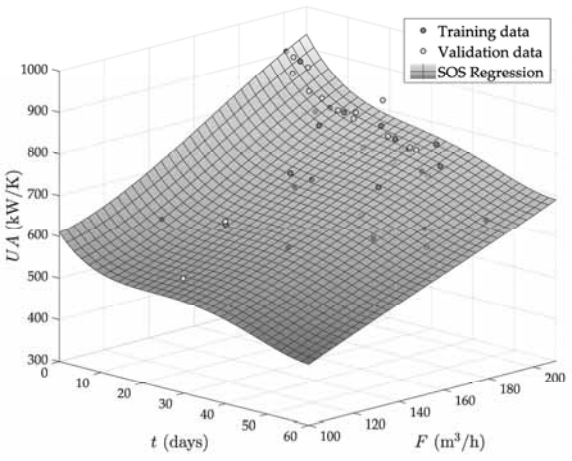
$$\begin{aligned} UA = {} & 7.06e^{-8}F_{SB}^4 + 2.95e^{-6}F_{SB}^3 t_{op} + \\ & 1.63e^{-6}F_{SB}^2 t_{op}^2 - 2.42e^{-6}F_{SB} t_{op}^3 + 1e^{-4} t_{op}^4 - \\ & 2e^{-4}F_{SB}^3 - 1.585e^{-3}F_{SB}^2 t_{op} + 5.1e^{-5}F_{SB} t_{op}^2 - \\ & 0.0138 t_{op}^3 + 0.089 F_{SB}^2 + 0.232 F_{SB} t_{op} + 0.627 t_{op}^2 - \\ & 10.87 F_{SB} - 22.78 t_{op} + 1000 \end{aligned} \quad (11)$$

4 Final Remarks

Digitalization in industrial sites is not just smart sensors, huge databases, and nice monitoring tools. In the authors' opinion, the step beyond current practice is to really extract and combine all the available process information to take better decisions in real time.



a) Fitting using software ALAMO



b) Fitting by SOS regression

Figure 6: Fitting the heat-transmission coefficient by constrained regression methods.

Method	Train. Err.	Val. Err.	Total	Decay
LS	14.452	15.226	29.719	7.17%
LS reg.	13.448	14.282	27.730	-
ALAMO	18.061	18.402	36.463	31.5%
SOS CR	14.751	13.362	28.113	1.38%

Table 1: Absolute least squared error to data accumulated by the presented models.

In this paper, the authors discussed how essential is incorporating process knowledge with sampled data in order to really extract sensible information, which can be later use for decision support in the process industry. For this task, model-based tests to detect (and improve) the data quality (robust DR methods in particular) as well as

constrained-regression approaches proven to be quite effective in our case study.

Constrained regression is especially relevant/useful when data is scarce, or when there are lots of samples but containing nearly the same information about the process. It is also worth to remark that incoherent model responses could be detected (and corrected ad-hoc perhaps) in two- or three-dimensional models, but this would be impossible in larger multidimensional systems.

Acknowledgement. This research received funding from the EU Horizon 2020 research and innovation programme under Grant No. 723575 (CoPro), and from the Spanish MICINN with FEDER funds via the research project InCO4In (PGC2018-099312-B-C31).

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